



**CHALMERS**  
UNIVERSITY OF TECHNOLOGY

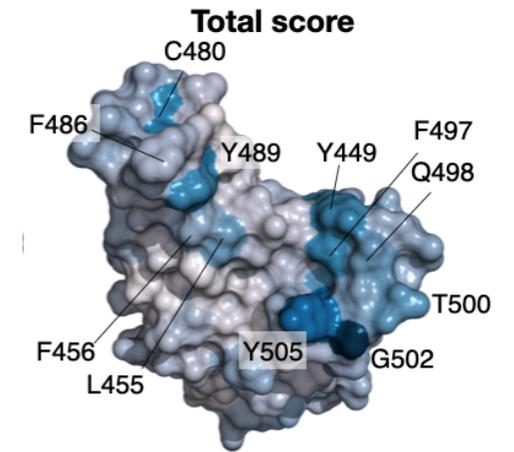
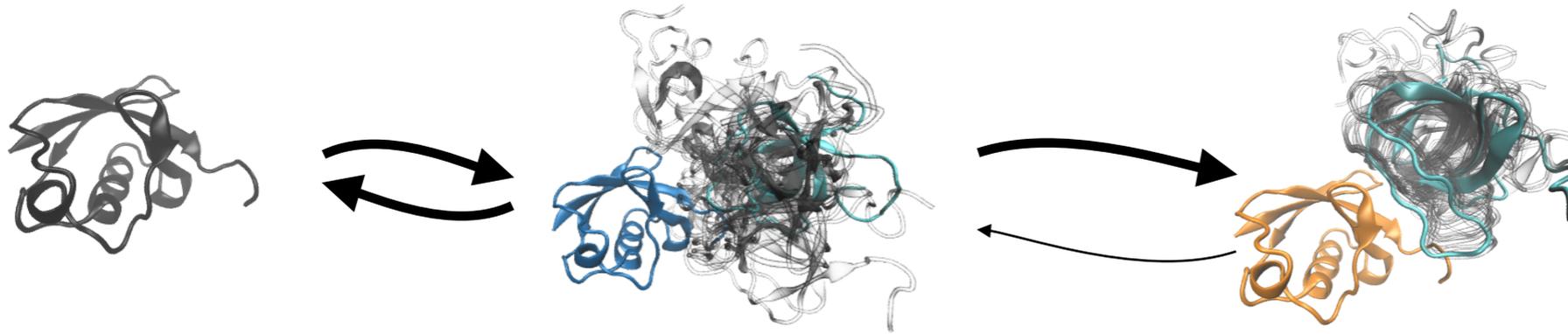
# AI and Machine Learning in the Natural Sciences

The WASP Winter Conference 2022

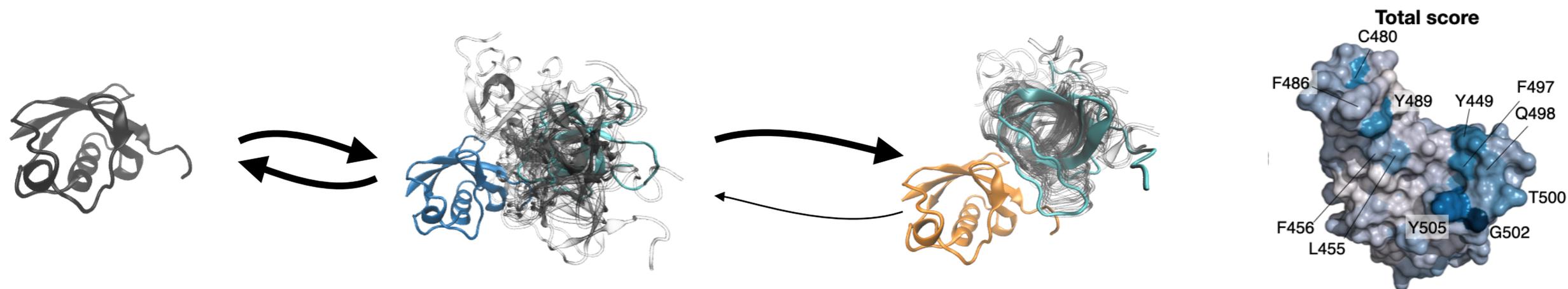
Simon Olsson

Data Science and AI, Computer Science and Engineering,  
Chalmers University of Technology

## Exciting applications — Molecular Design

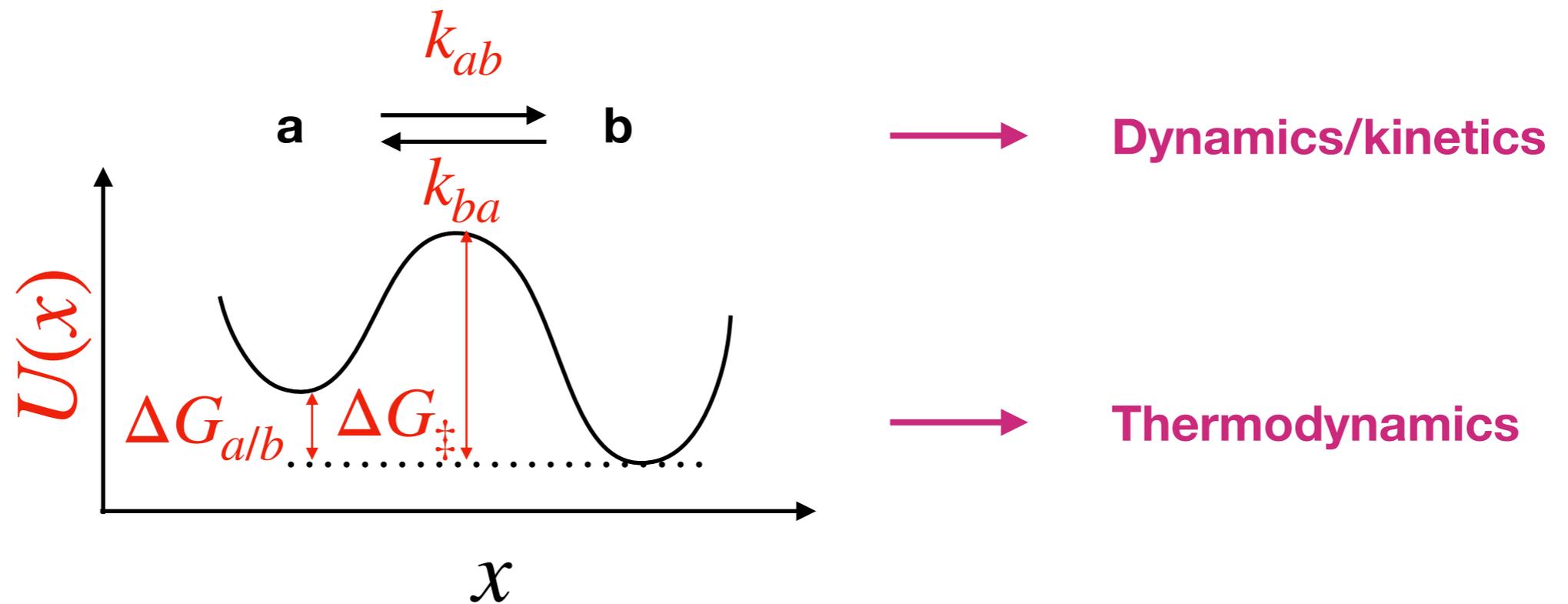


## Exciting applications — Molecular Design

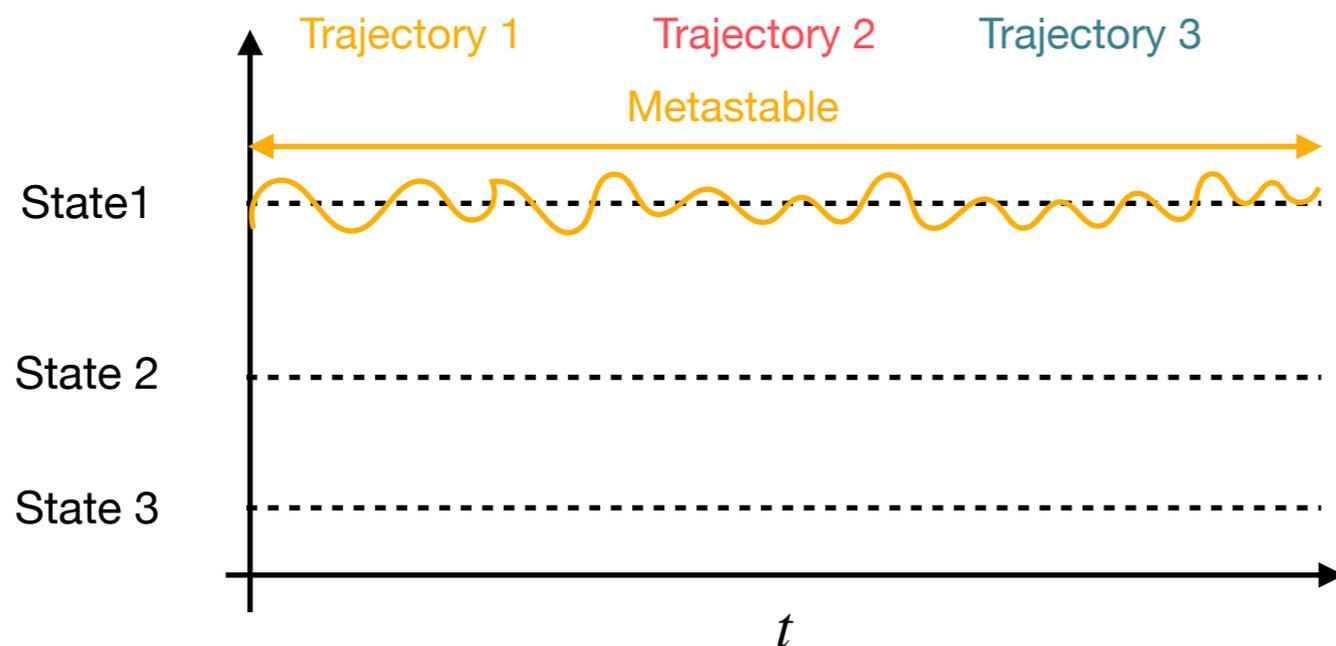
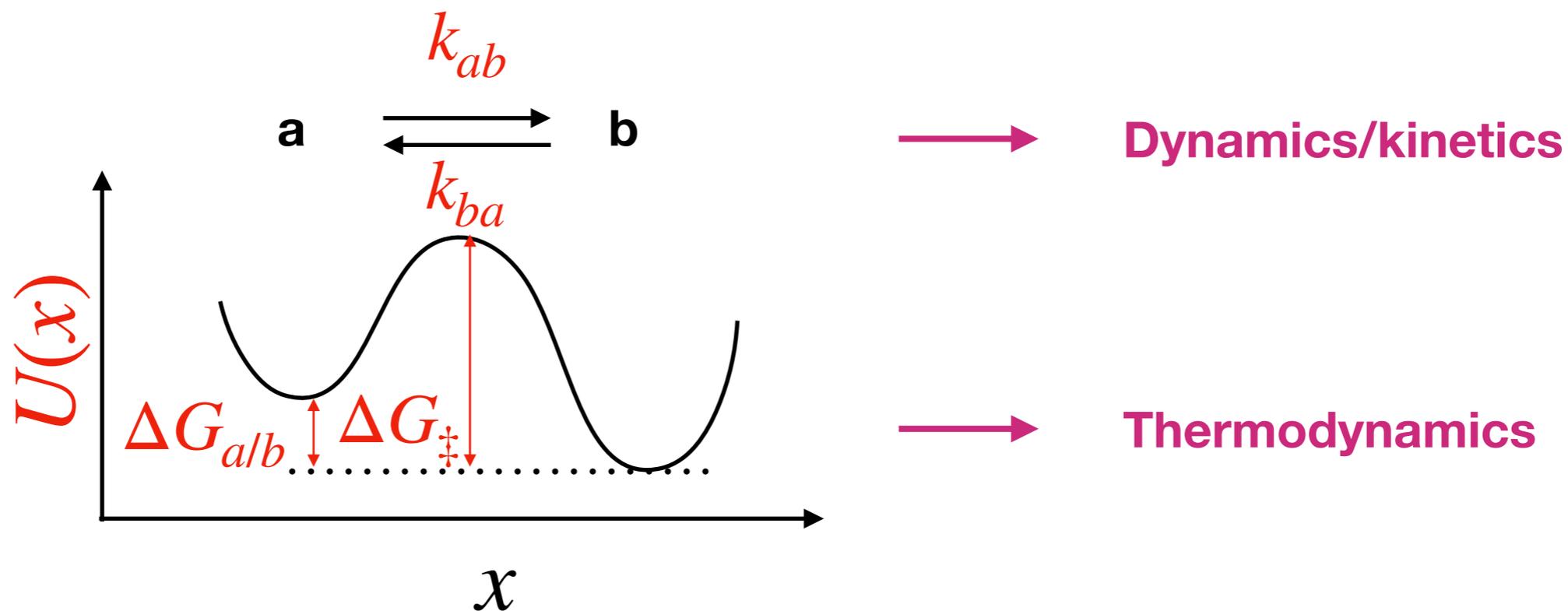


Tobias  
Karlsson

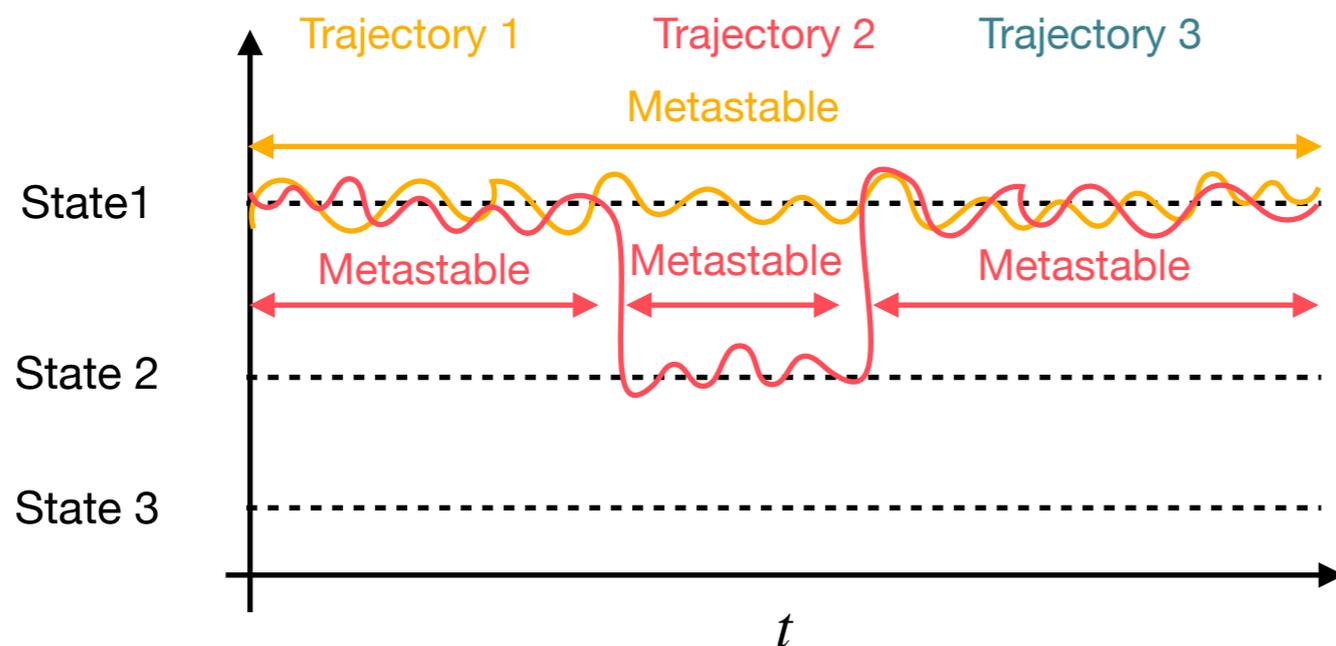
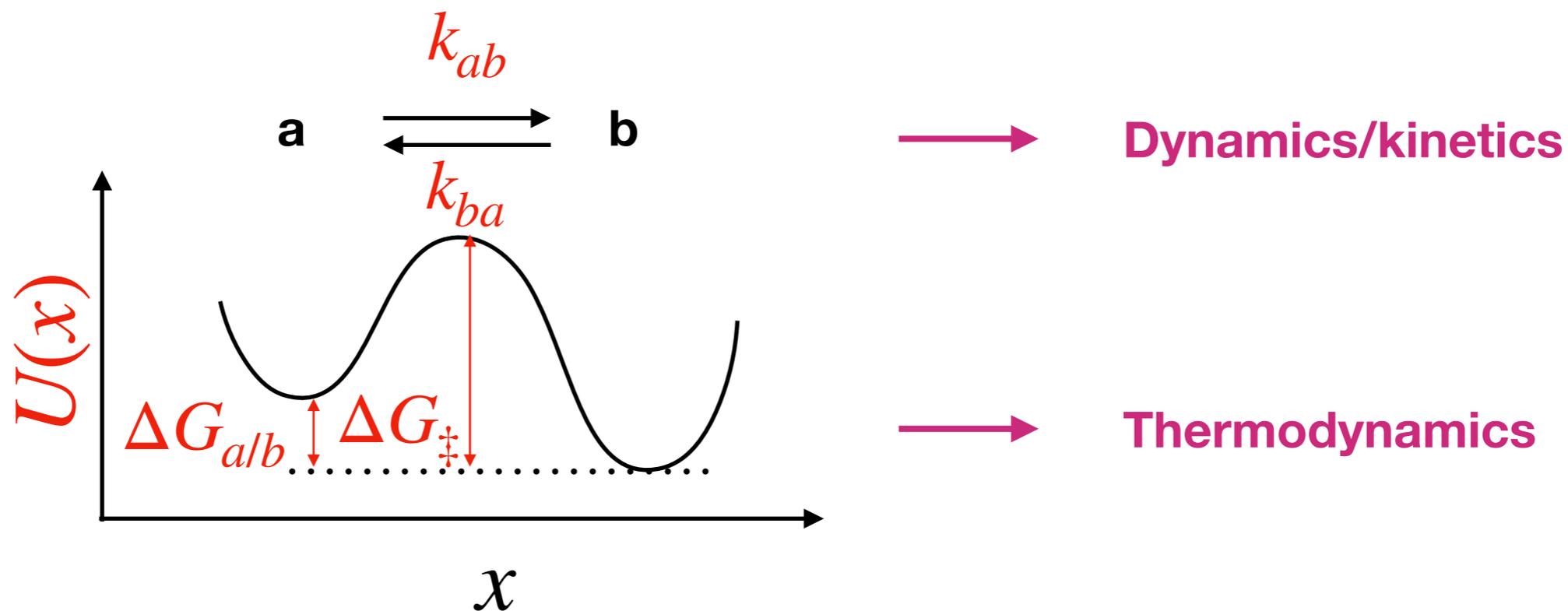
## Exciting applications — Efficient simulations



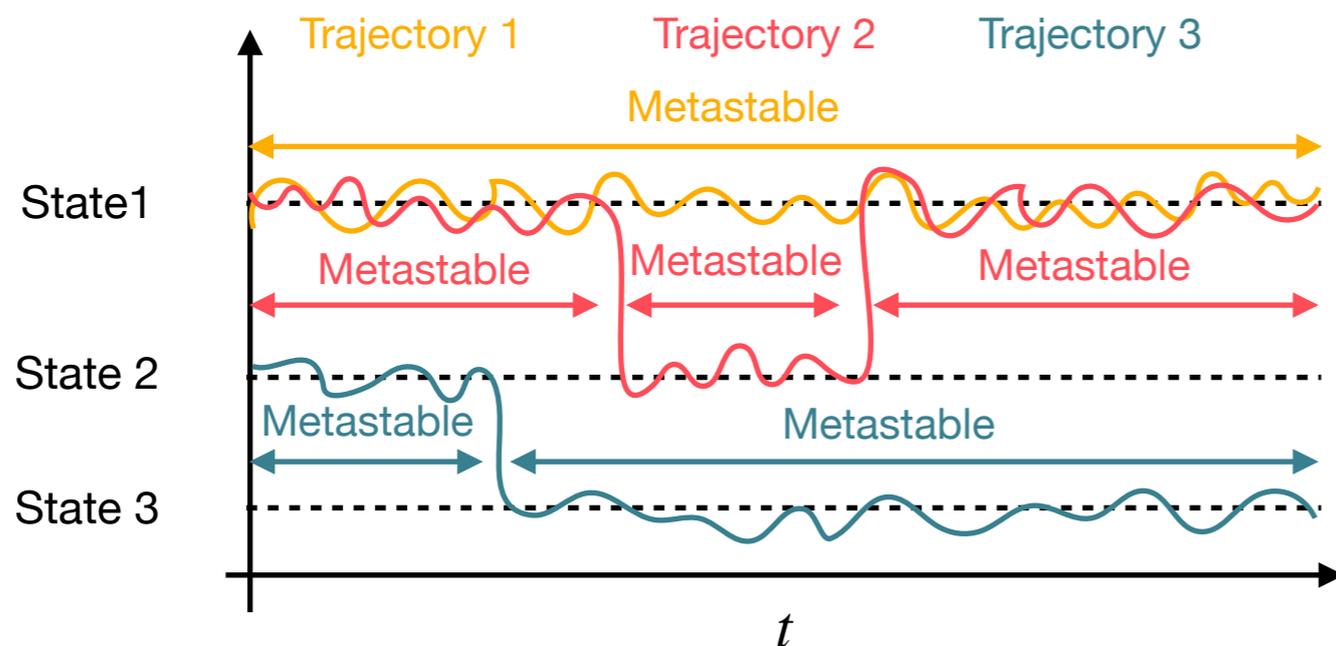
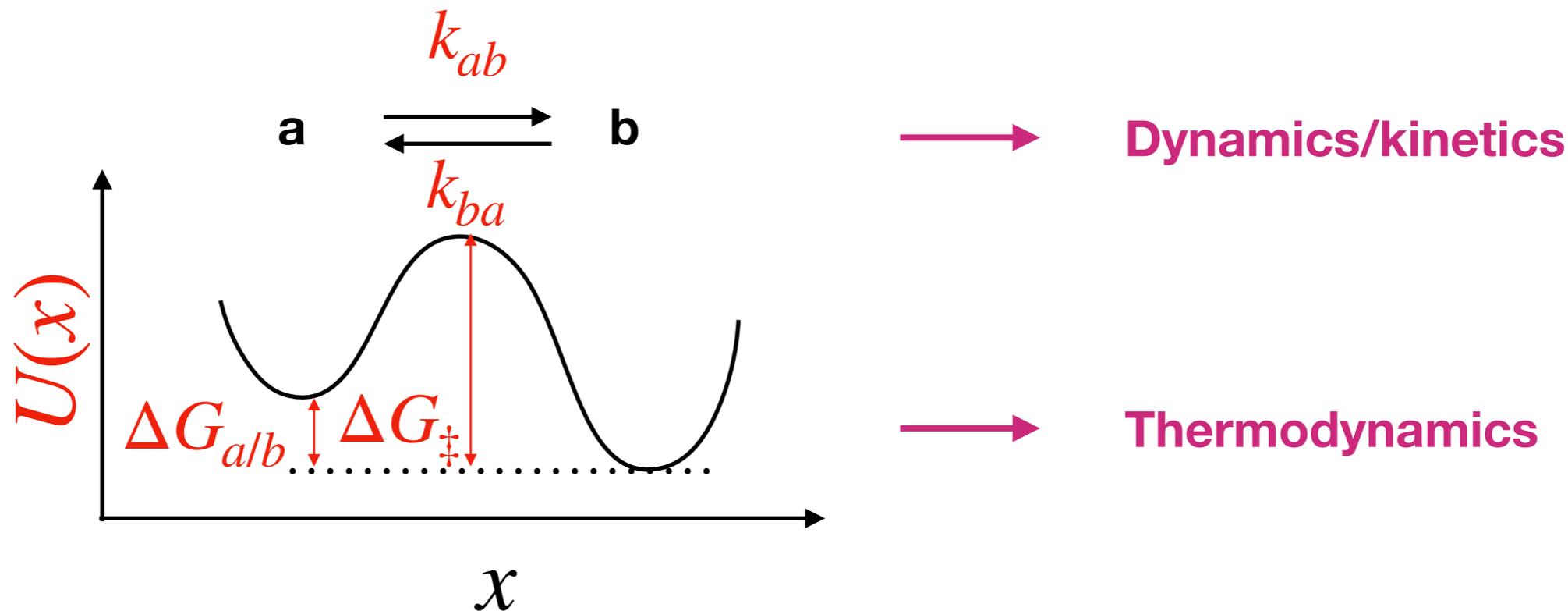
## Exciting applications — Efficient simulations



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## Exciting applications — Efficient simulations



### Non-IID data

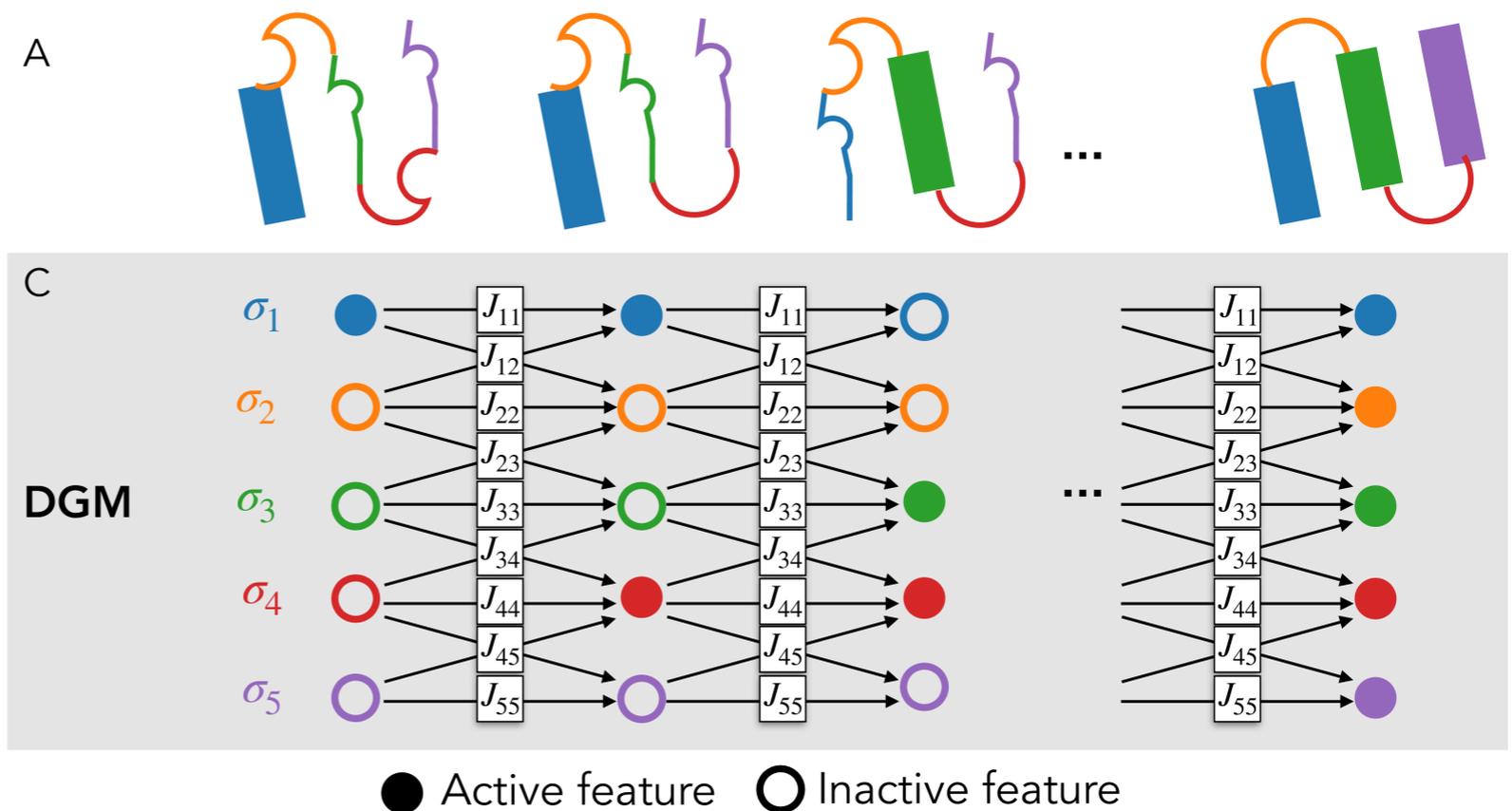
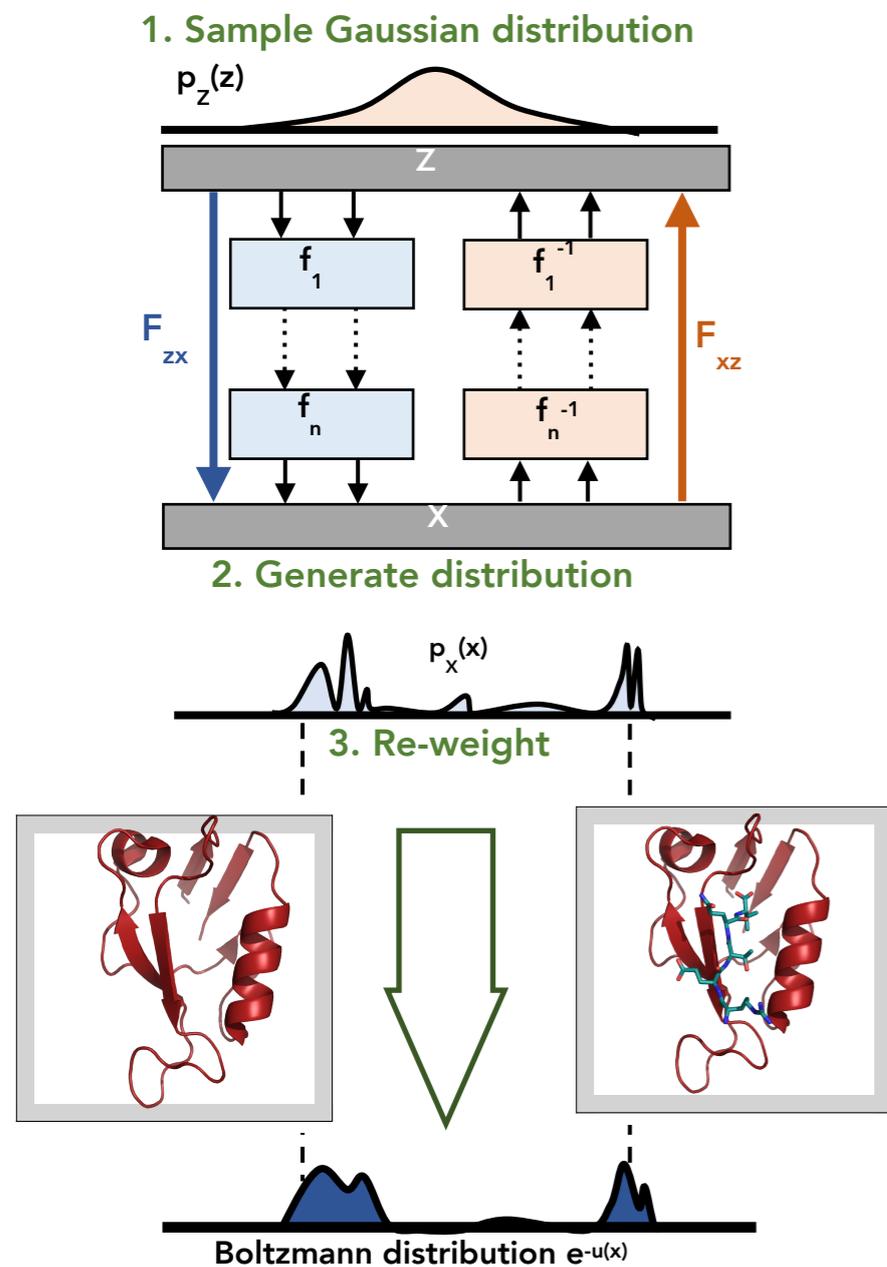


Juan Viguera Diez



Christopher Kolloff

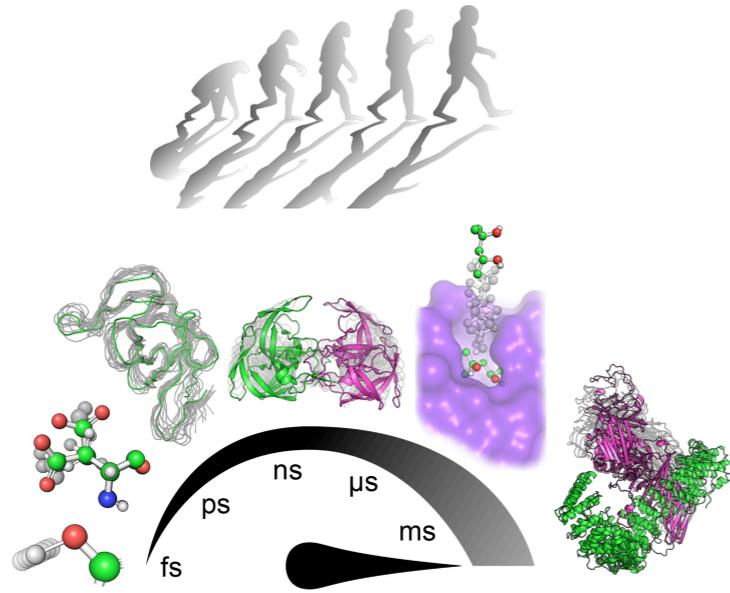
## Exciting applications — Efficient simulations



# AI and Machine learning in the Natural Sciences — why?

## Challenging theory

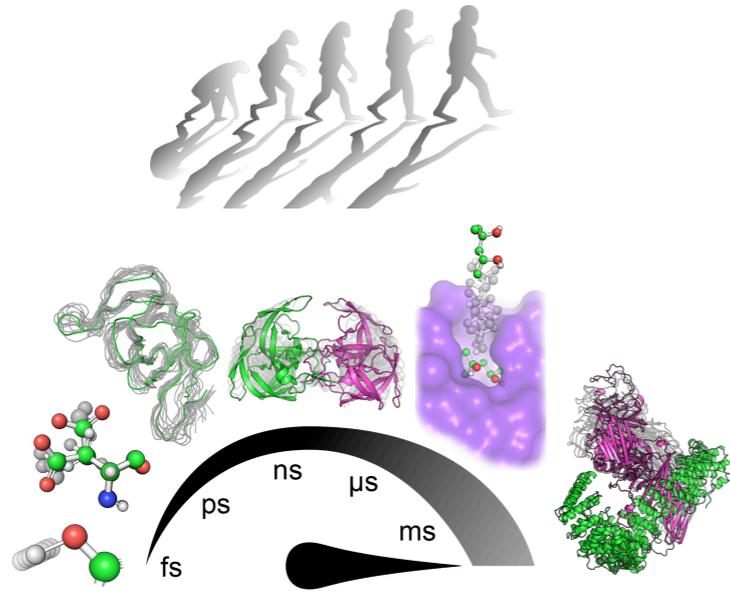
### Generative processes



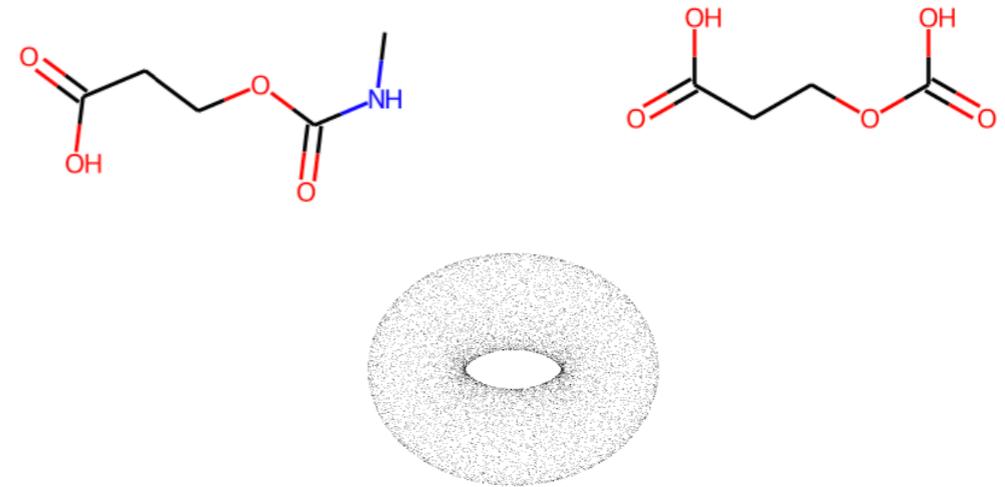
# AI and Machine learning in the Natural Sciences — why?

## Challenging theory

### Generative processes



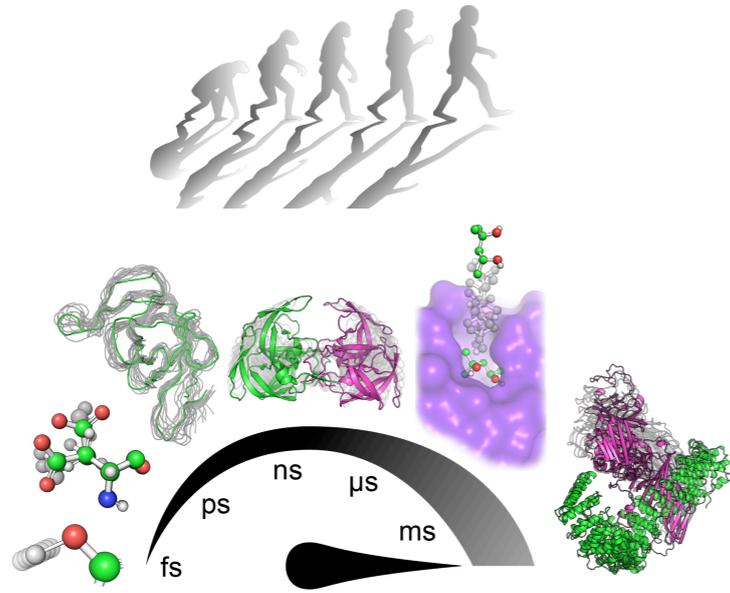
### Non-Euclidean data



# AI and Machine learning in the Natural Sciences — why?

## Challenging theory

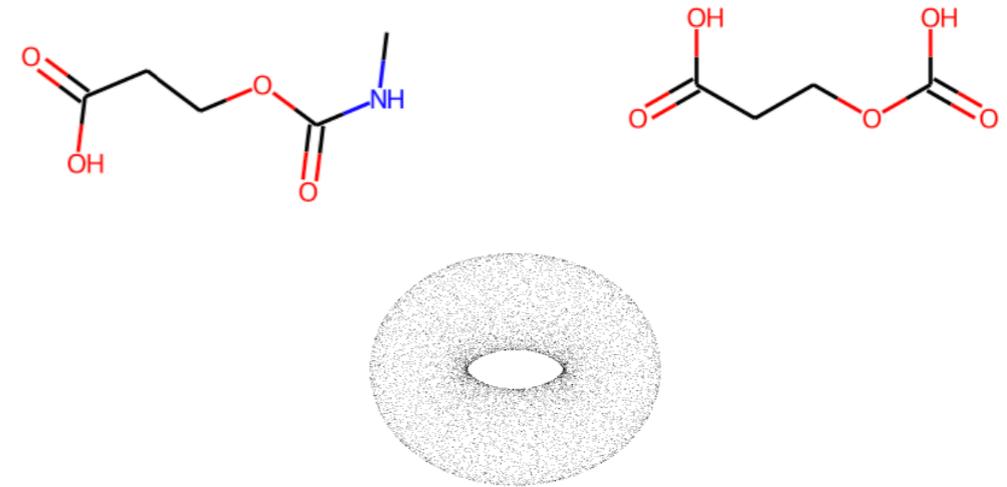
### Generative processes



### Domain adaptation/transfer learning

$$\mathbb{E}_{x \sim \mathcal{M}_1} [|f(x, M_1) - M_1(x)|_2] \approx \mathbb{E}_{x \sim \mathcal{M}_2} [|f(x, M_2) - M_2(x)|_2]$$

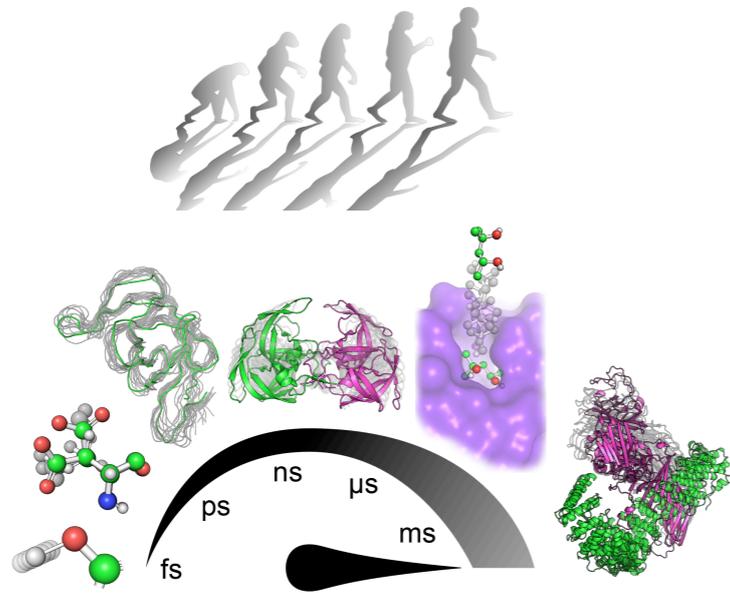
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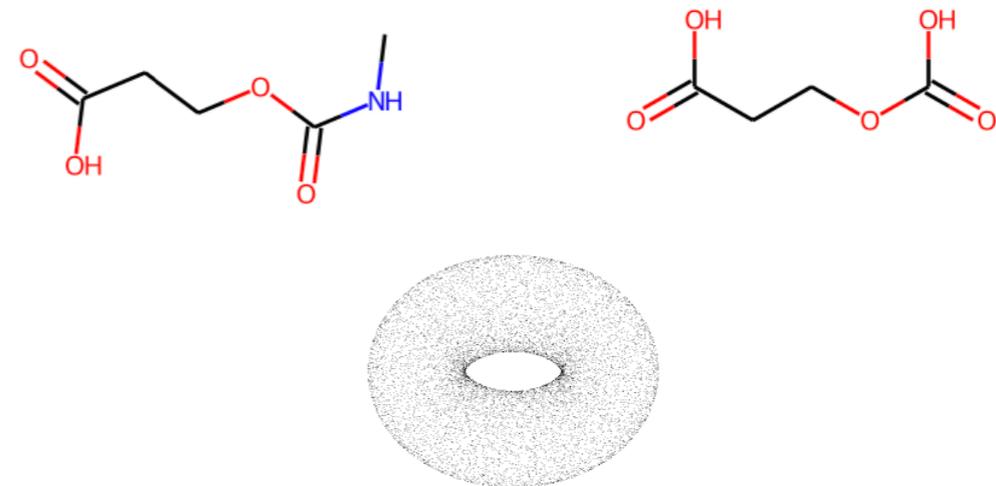
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### Non-Euclidean data



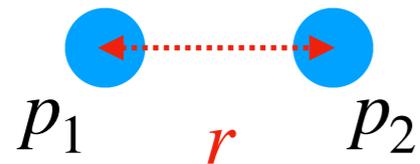
### Causal modeling



# What do know about our data?

**Potential energy:**

$$U(p_1, p_2) = (x_1 - x_2)^2 + (y_1 - y_2)^2 \\ = r^2$$



**Force:**

$$F = -\nabla U(p_1, p_2) \\ = -\left[ \left( \frac{\partial U}{\partial x_1}, \frac{\partial U}{\partial y_1} \right), \left( \frac{\partial U}{\partial x_2}, \frac{\partial U}{\partial y_2} \right) \right]$$

# What do know about our data?

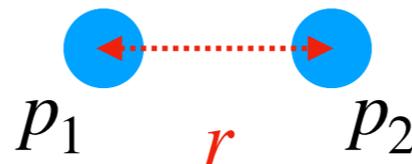
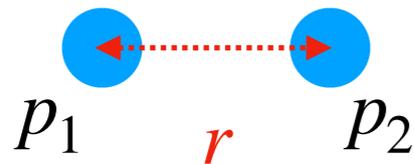
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**Translation**



# What do know about our data?

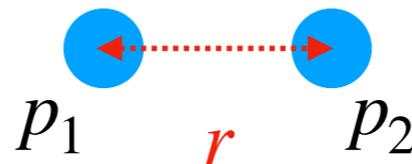
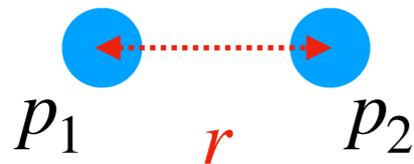
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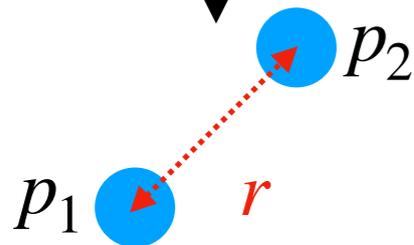
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**Translation**



**Rotation**



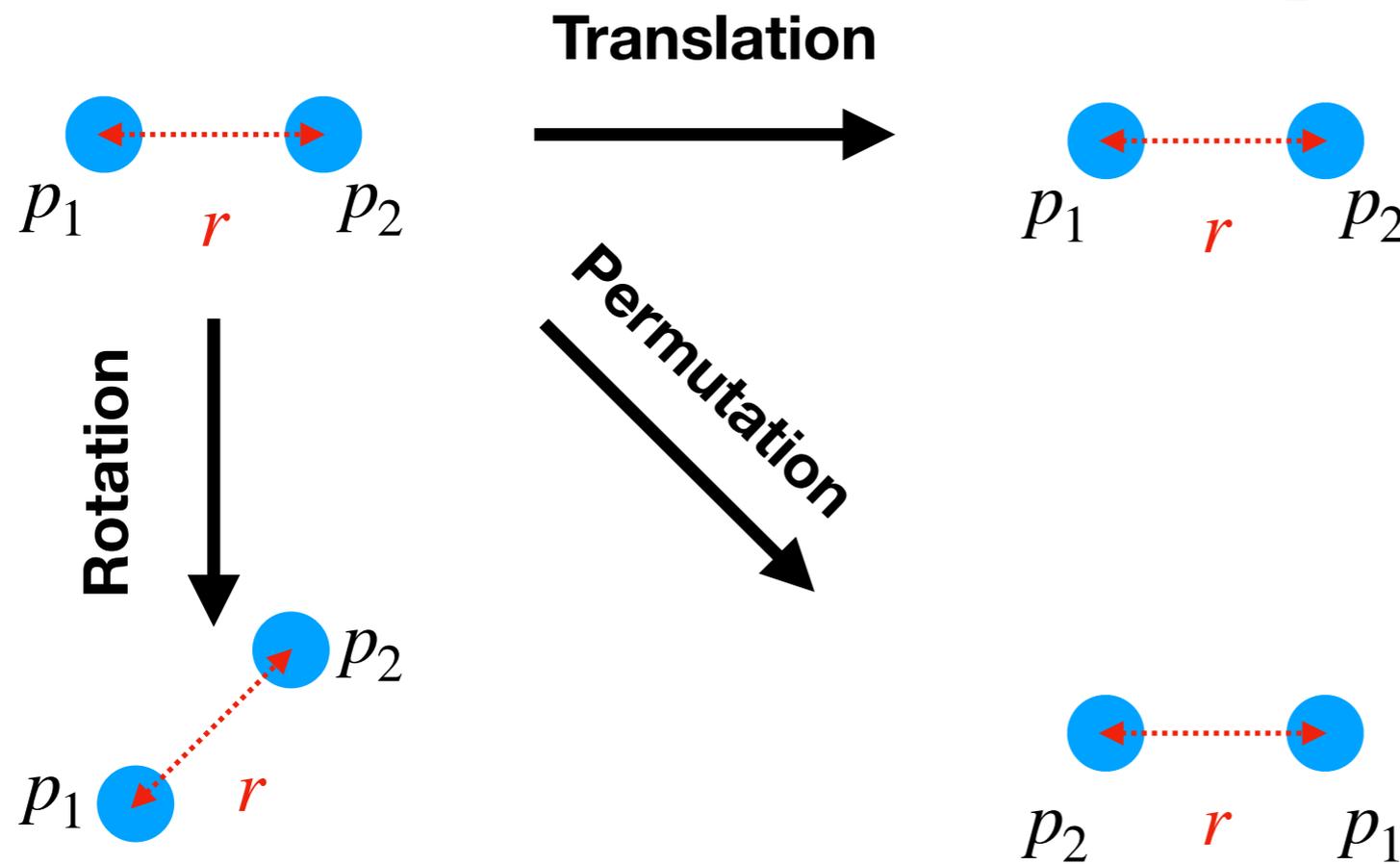
# What do know about our data?

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**What happens to the potential energy — and what about the force?**

# Noethers theorem — informally

*“If a system has a continuous symmetry property, then there are corresponding quantities whose values are conserved in time.”*



**Emmy Noether**

# Noethers theorem – informally

*“If a system has a continuous symmetry property, then there are corresponding quantities whose values are conserved in time.”*

**Symmetry  $\Leftrightarrow$  Conservation Law**



**Emmy Noether**

# A transferable Boltzmann Generator for small molecules



**Juan Viguera Diez**

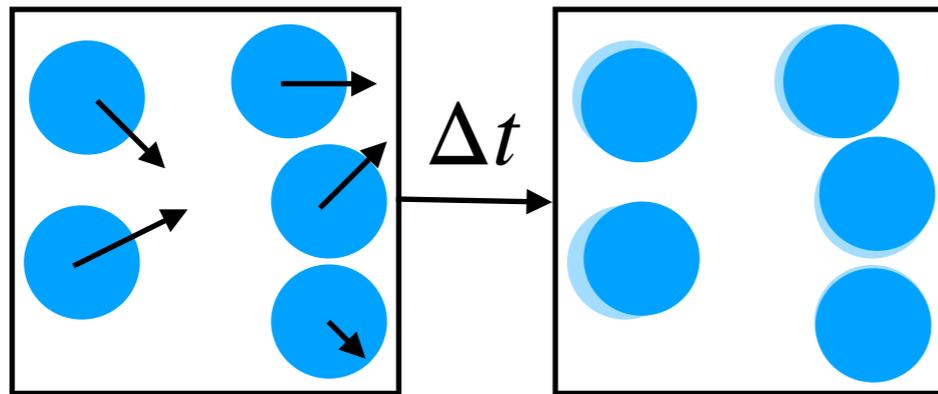


**Sara Romeo Atance**

**Challenge:**  $\mathbf{x} \sim p(\mathbf{x}) \propto \exp(-\beta U(\mathbf{x}))$

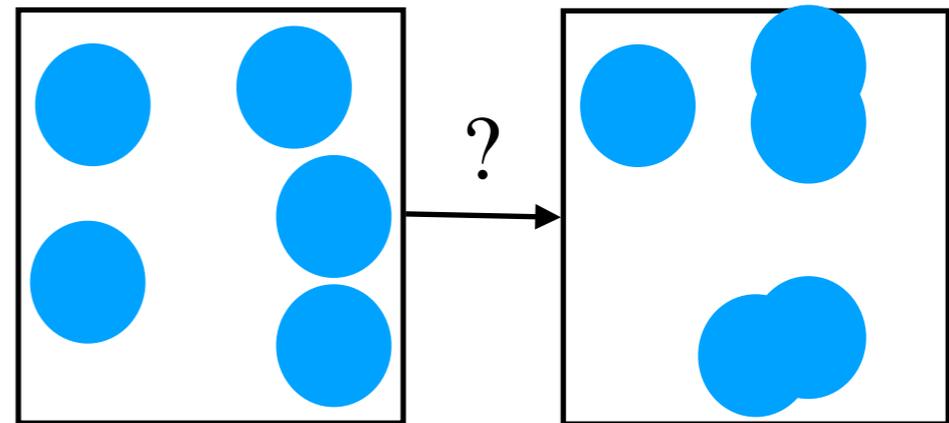
**Challenge:**  $\mathbf{x} \sim p(\mathbf{x}) \propto \exp(-\beta U(\mathbf{x}))$

## Molecular dynamics



Correlated samples = *Slow mixing*

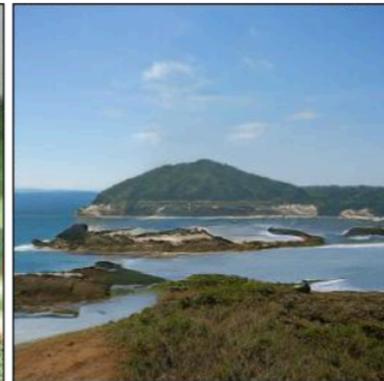
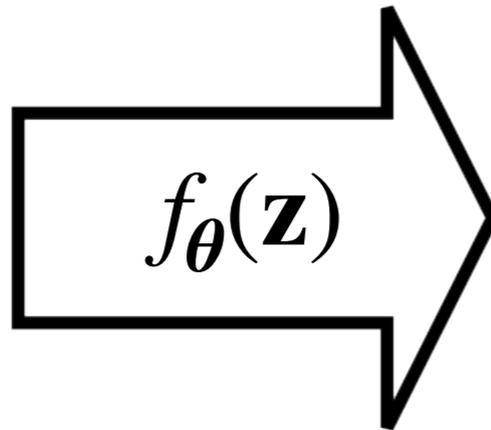
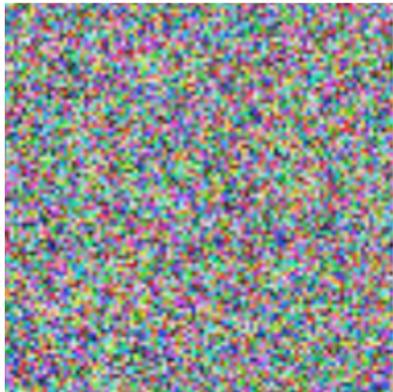
## Monte Carlo



Low-acceptance or  
highly correlated samples

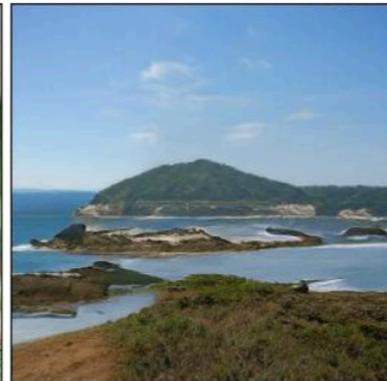
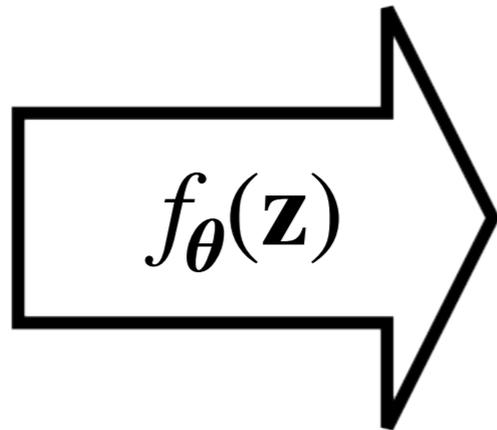
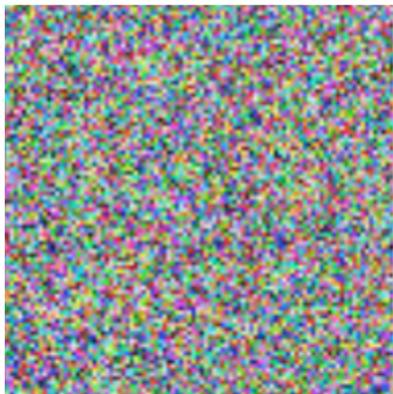
# Deep Generative Models

$$\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

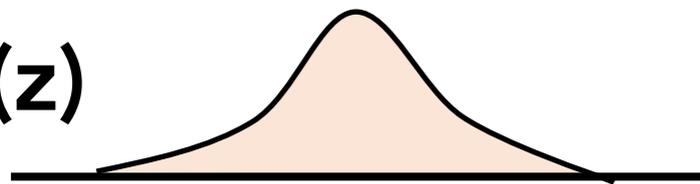


# Deep Generative Models

$$\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$



$$p_{\mathbf{z}}(\mathbf{z})$$

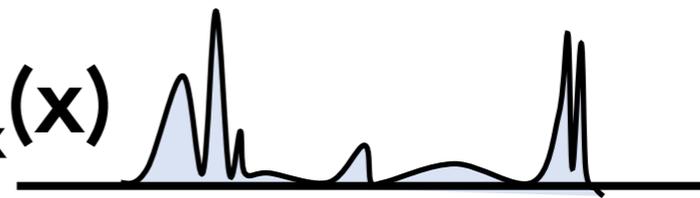


Prior distribution

$$\mathbf{x} = f_{\theta}(\mathbf{z})$$



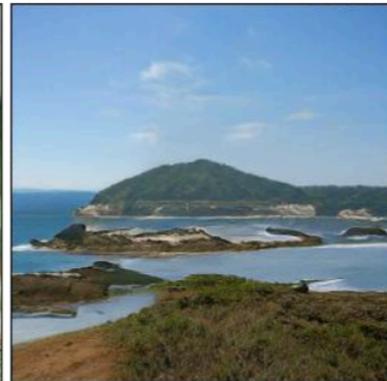
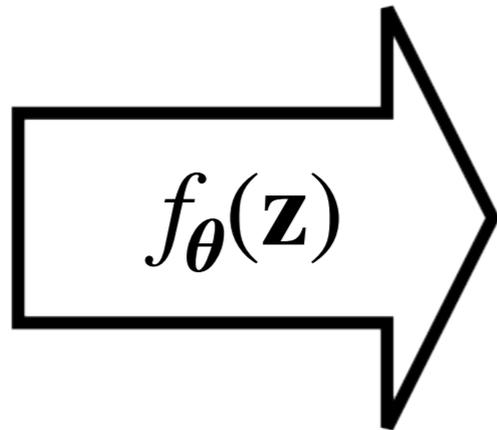
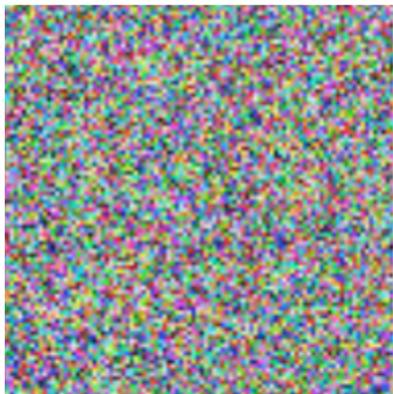
$$p_{\mathbf{x}}(\mathbf{x})$$



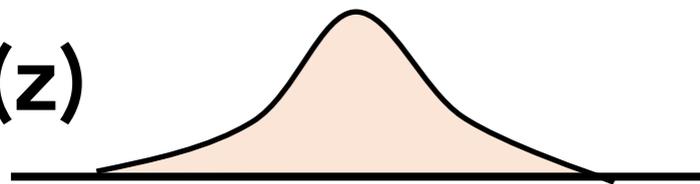
Distribution of images

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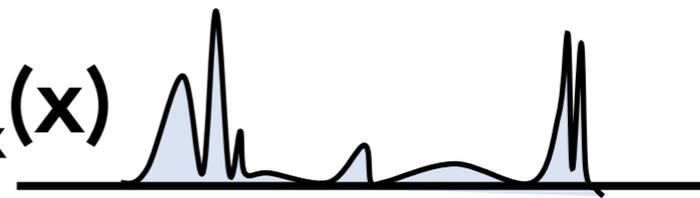


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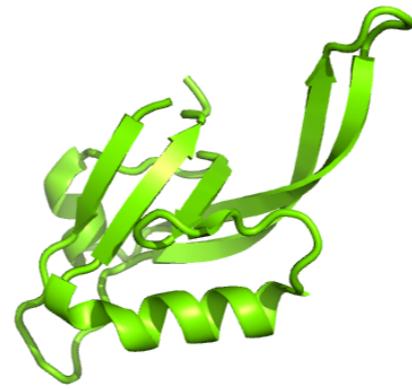
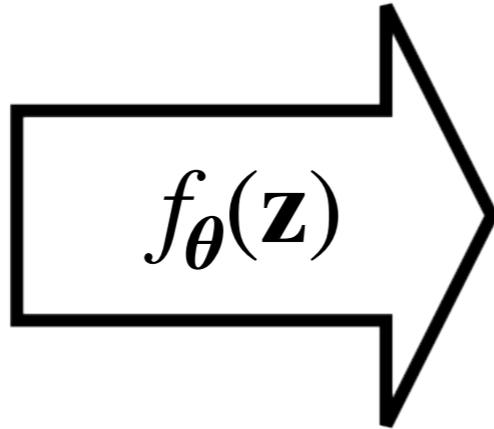
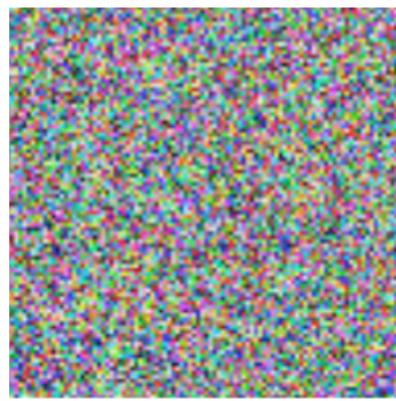
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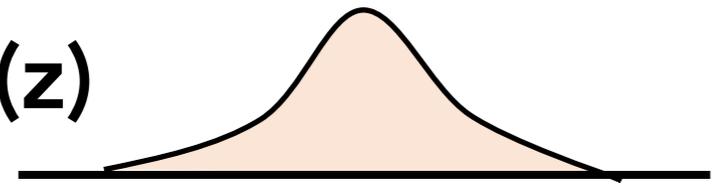
Distribution of images

**What if  $p_{\mathbf{x}}(\mathbf{x})$  was the Boltzmann distribution?**

$$\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbb{I})$$



$$p_{\mathbf{z}}(\mathbf{z})$$

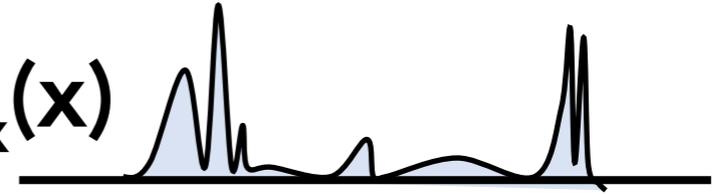


Prior distribution

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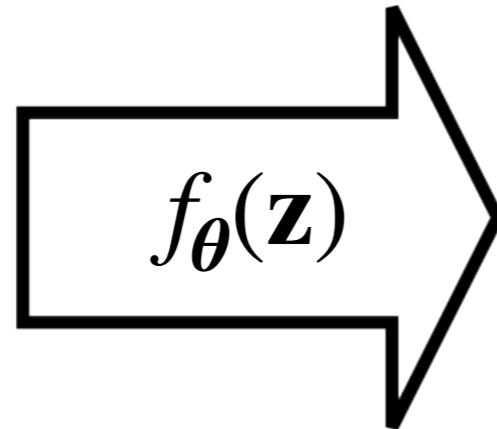
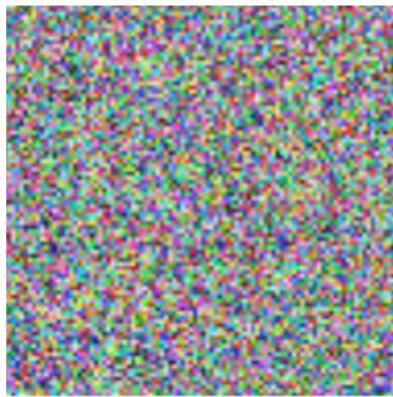


$$p_{\mathbf{x}}(\mathbf{x})$$

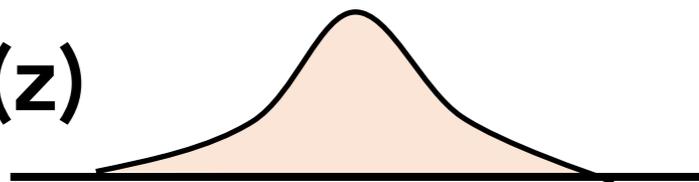


Boltzmann distribution?

$$\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbb{I})$$



$$p_z(\mathbf{z})$$

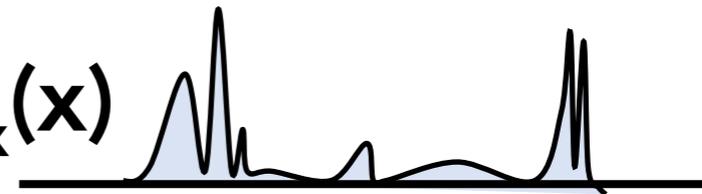


Prior distribution

$$\mathbf{x} = f_\theta(\mathbf{z})$$



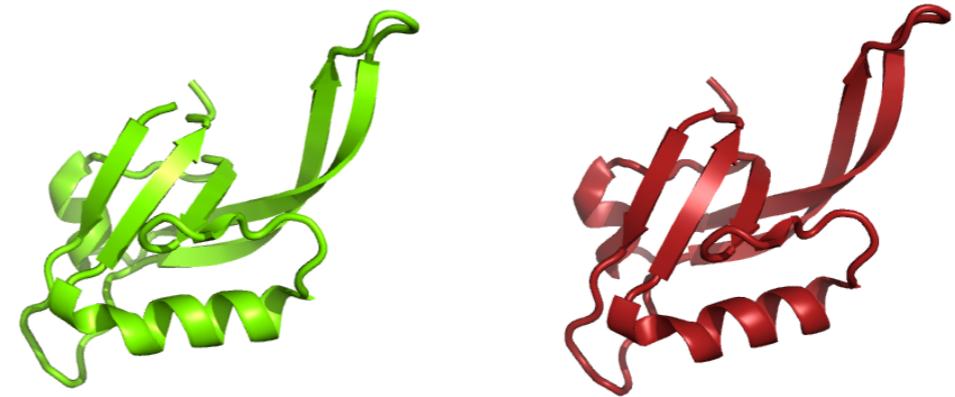
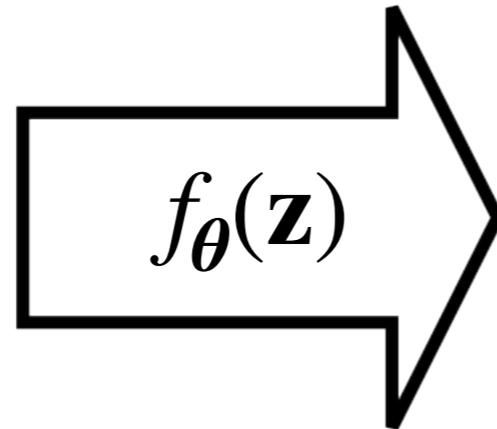
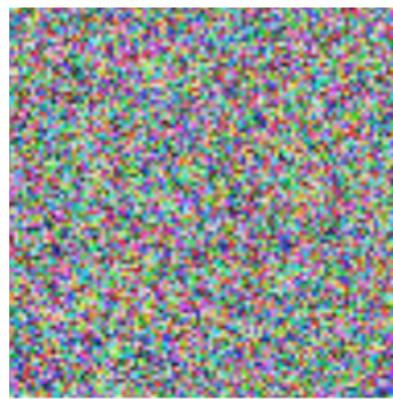
$$p_x(\mathbf{x})$$



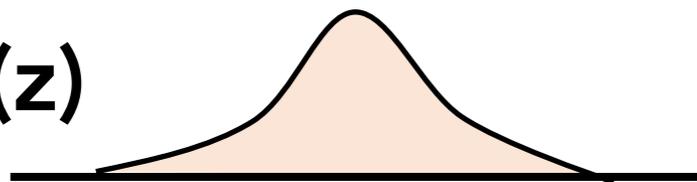
Boltzmann distribution?

Problem: We do not have a lot of data!

$$\mathbf{z} \sim \mathcal{N}(0, \mathbb{I})$$



$$p_z(\mathbf{z})$$

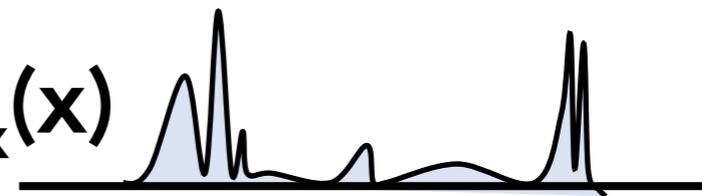


Prior distribution

$$\mathbf{x} = f_\theta(\mathbf{z})$$



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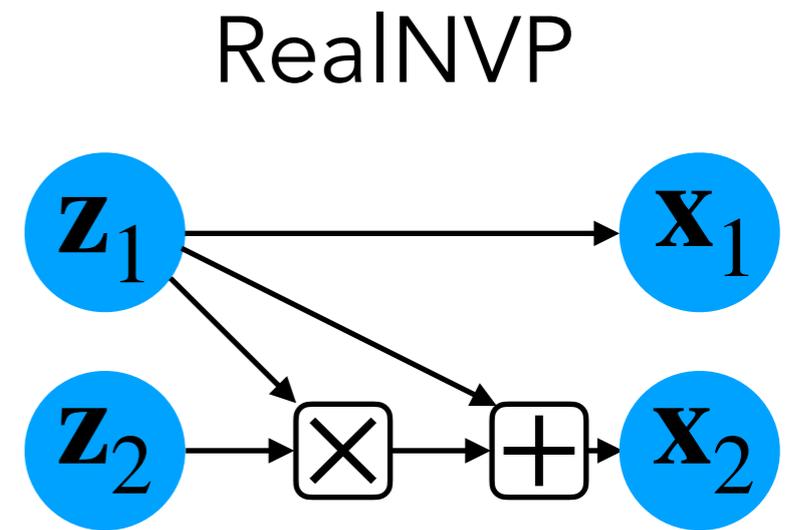
Boltzmann distribution?

Problem: We do not have a lot of data!

But we do have  $U(\mathbf{x})$

If  $f_{\theta}(\mathbf{z})$  satisfies + cheap to compute

$$\begin{aligned} \mathbf{x} &= f_{\theta}(\mathbf{z}) & J(\mathbf{z}) \\ \mathbf{z} &= f_{\theta}^{-1}(\mathbf{x}) & J^{-1}(\mathbf{x}) \end{aligned}$$



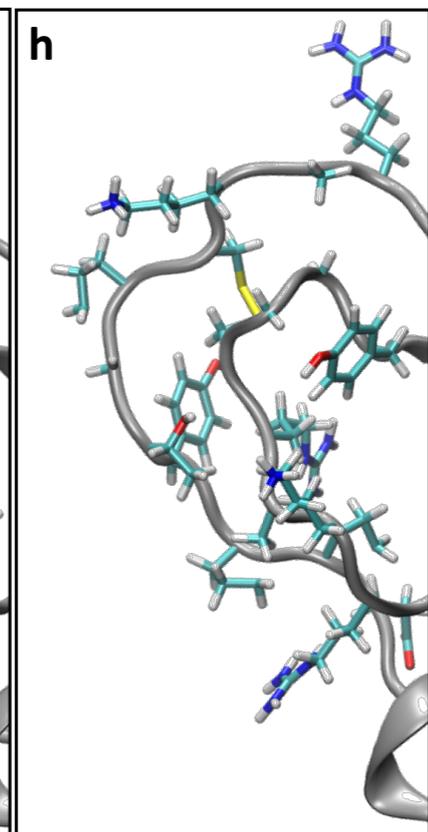
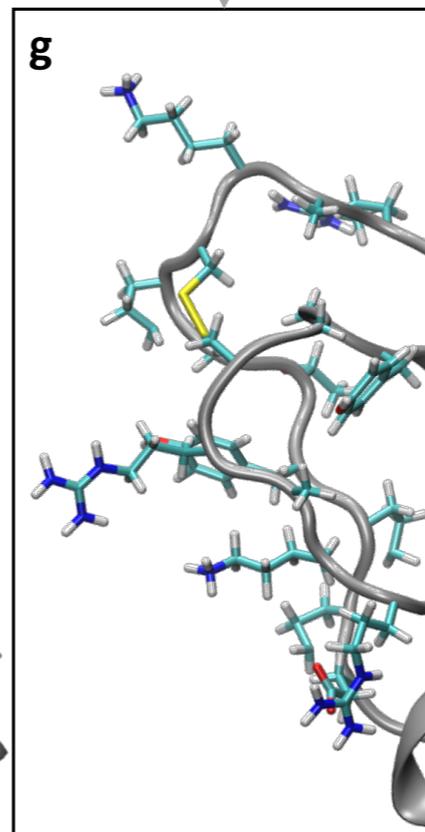
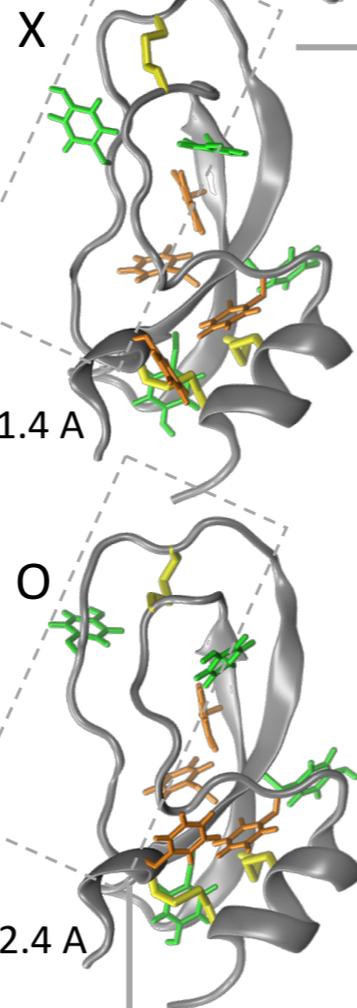
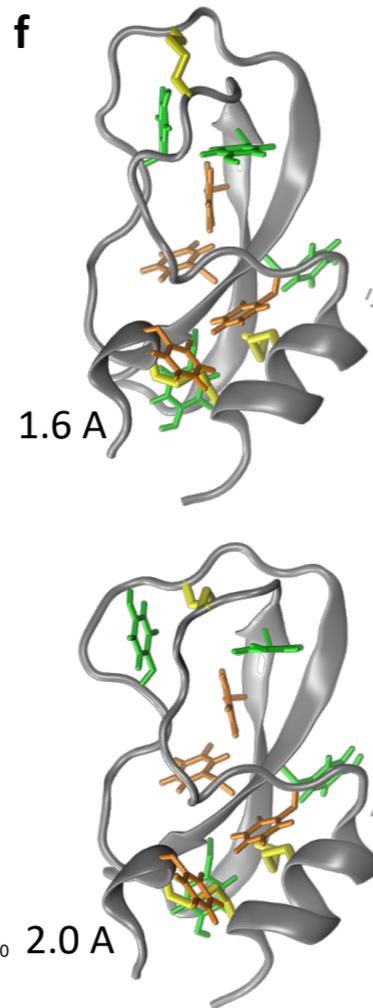
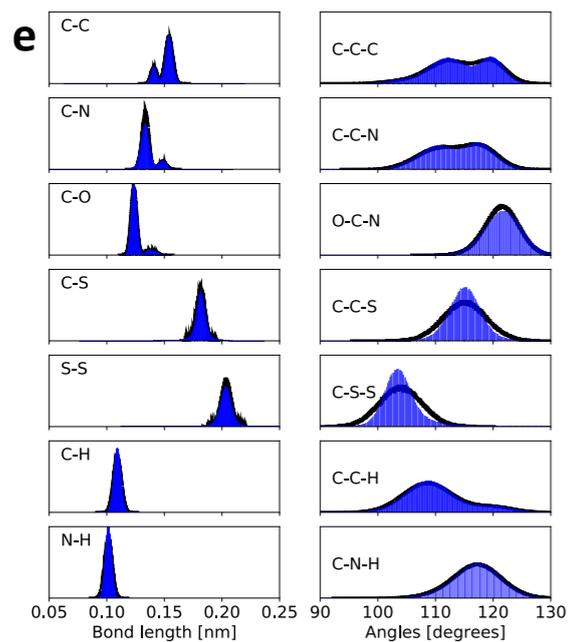
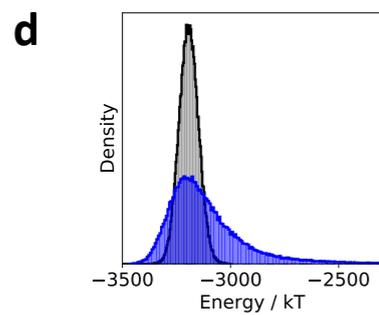
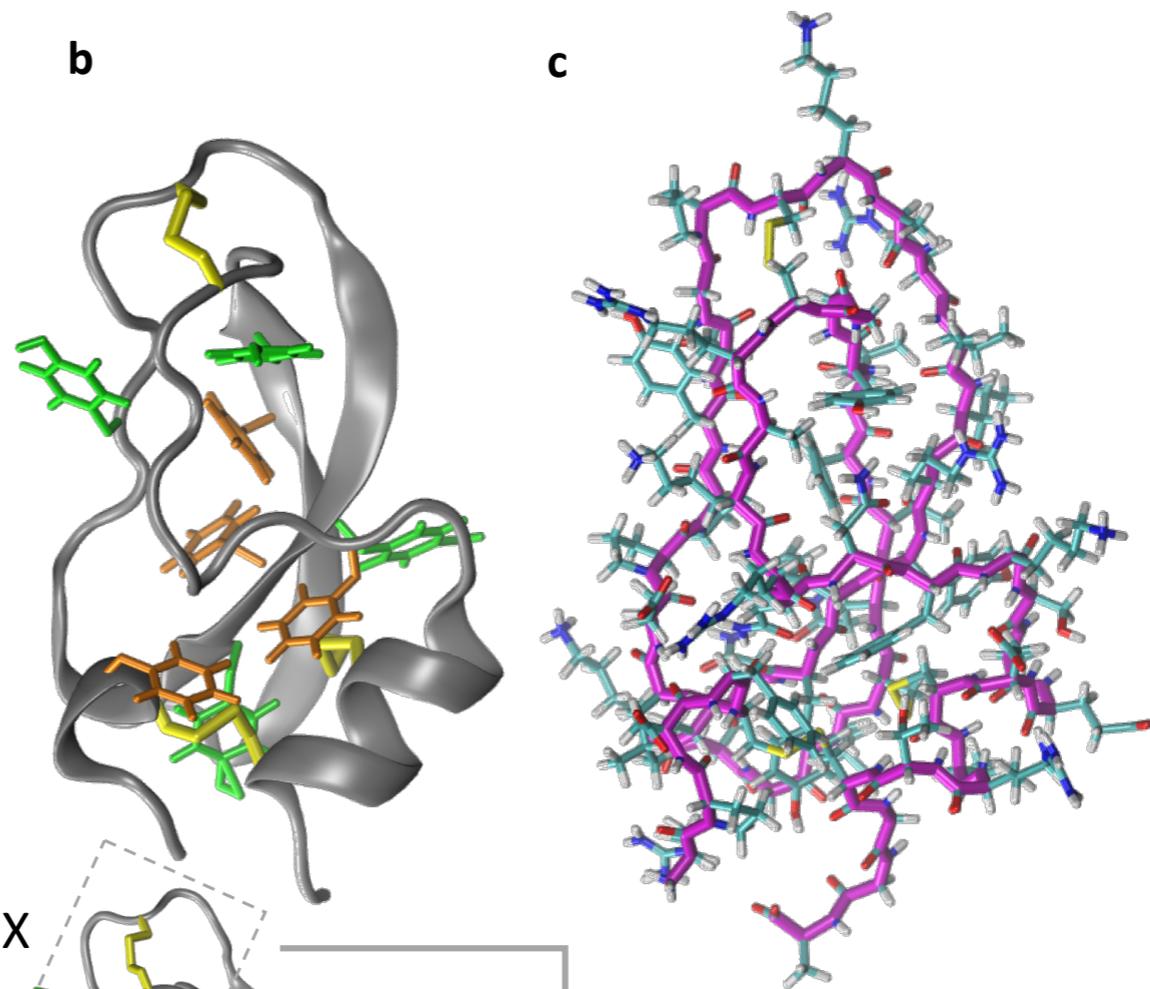
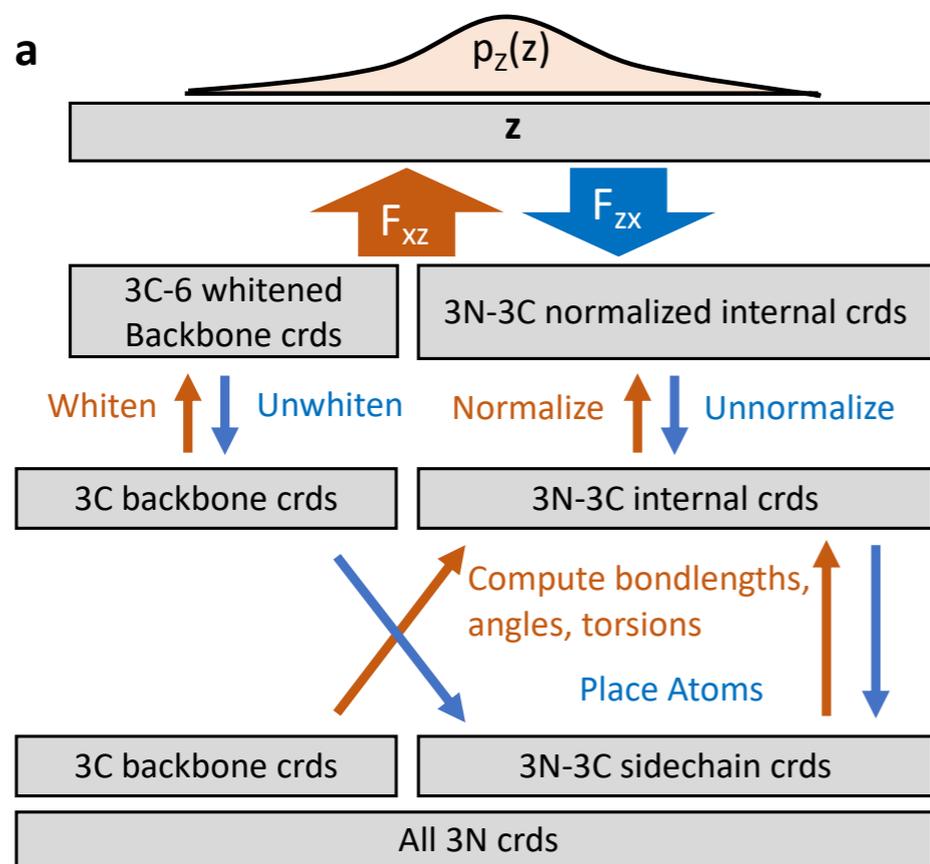
Dinh, Sohl-Dickstein & Bengio *arXiv:1605.08803* (2016).

We can optimize

$$J_{KL} = \mathbb{E}_{\mathbf{z} \sim p(\mathbf{z})} [U(f_{\theta}(\mathbf{z})) - \log \det J(\mathbf{z})]$$

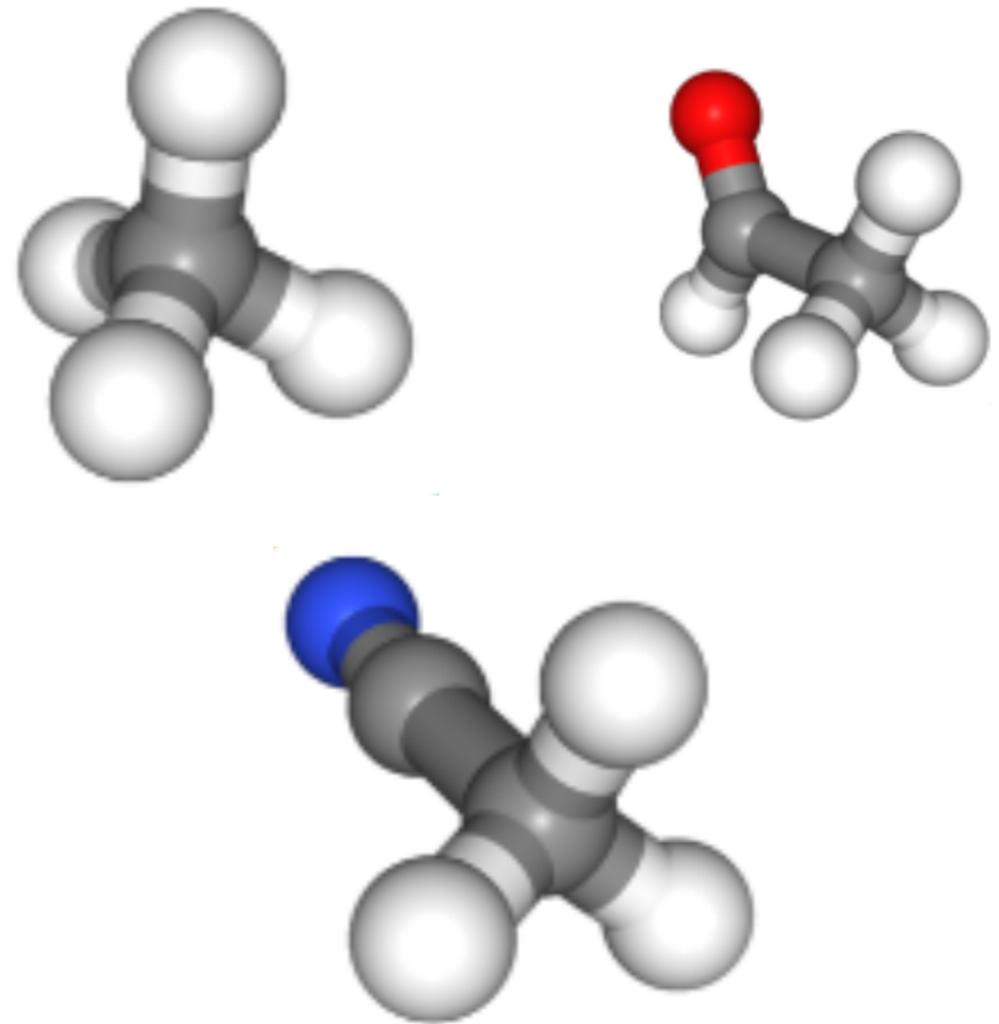
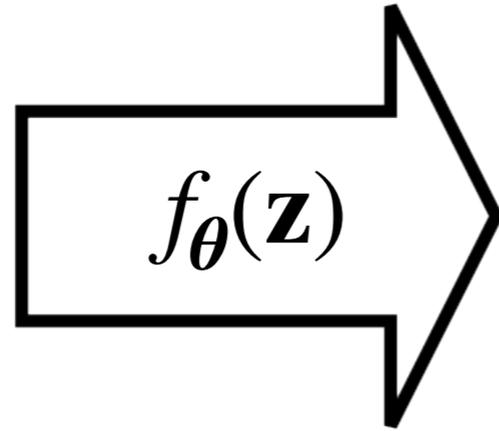
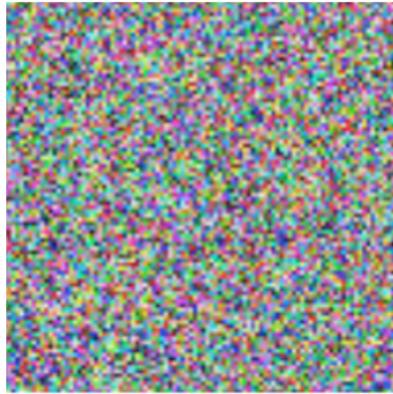
Potential energy  
(‘enthalpy’)

Smearing of prior distribution  
(‘entropy’)



How can we build a Boltzmann Generator which works for multiple molecules?

$$\mathbf{z} \sim \mathcal{N}(0, \mathbb{I})$$



How can we build a Boltzmann Generator which works for multiple molecules?

**Use an auto-regressive structure,**

$$p_{\theta, M}(\mathbf{x}) = p(\mathbf{x}_1) \prod_{i=2}^N p(\mathbf{x}_i | \mathbf{x}_{<i})$$

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**Use an auto-regressive structure,**

$$p_{\theta, M}(\mathbf{x}) = p(\mathbf{x}_1) \prod_{i=2}^N p(\mathbf{x}_i | \mathbf{x}_{<i})$$

**Transferable kernel,**

$$p_{\theta, M}(\mathbf{x}) = \prod_{i=2}^N p_{\theta}(\mathbf{x}_i | \mathbf{C}_i)$$

**With  $\mathbf{C}_i = (\mathbf{M}, \mathbf{A}_i, \mathbf{R}_{<i}, \mathbf{F}_i)$**

# How can we build a Boltzmann Generator which works for multiple molecules?

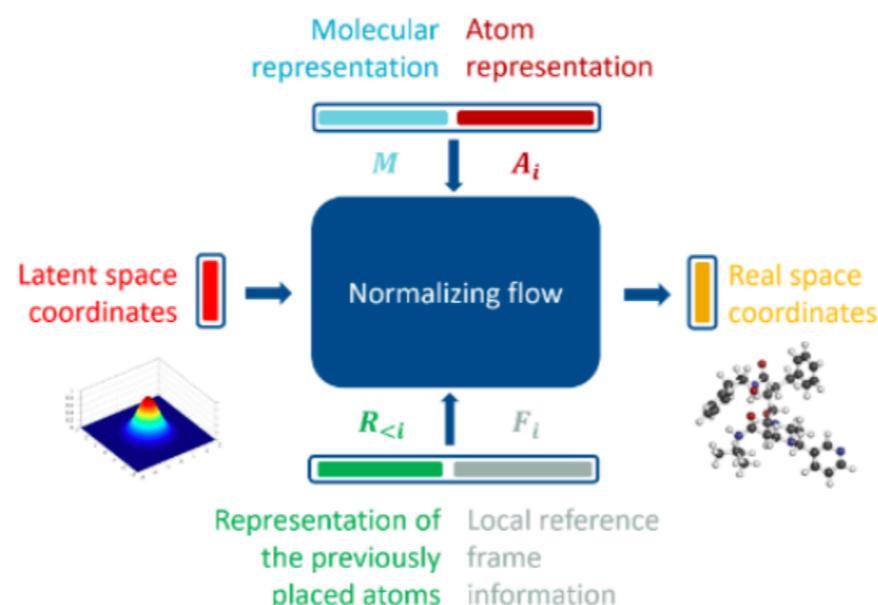
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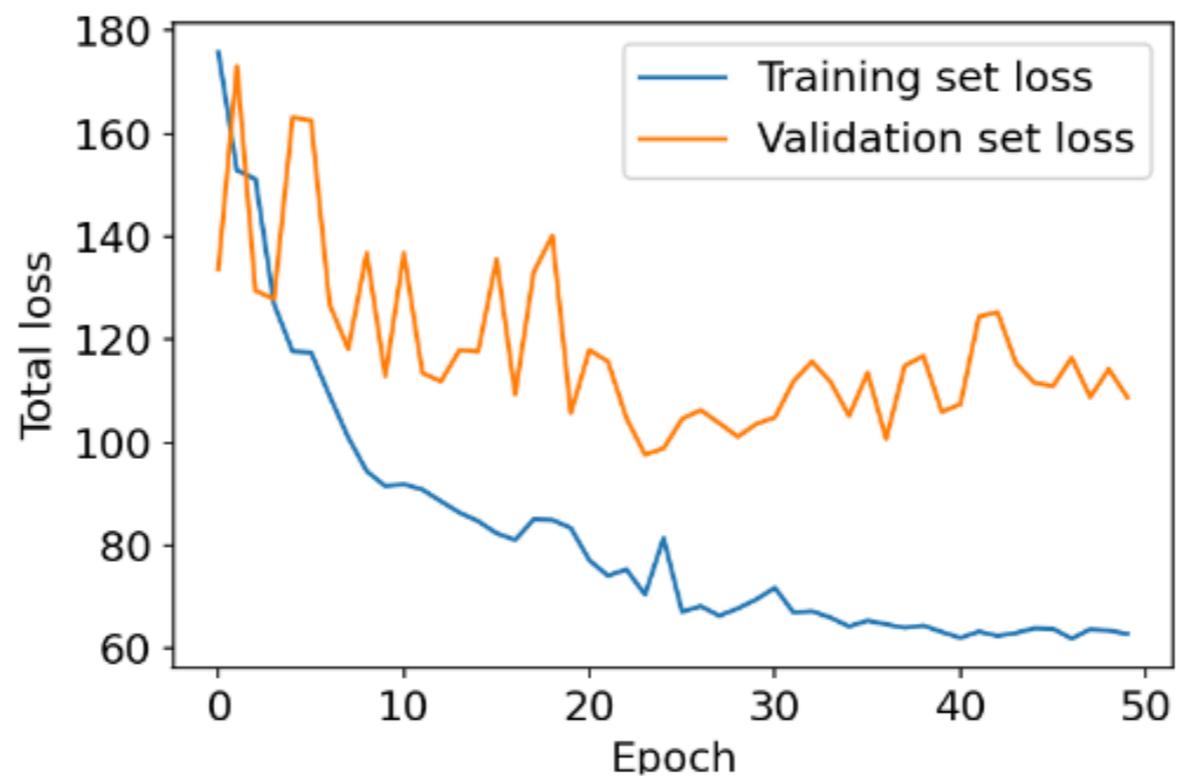
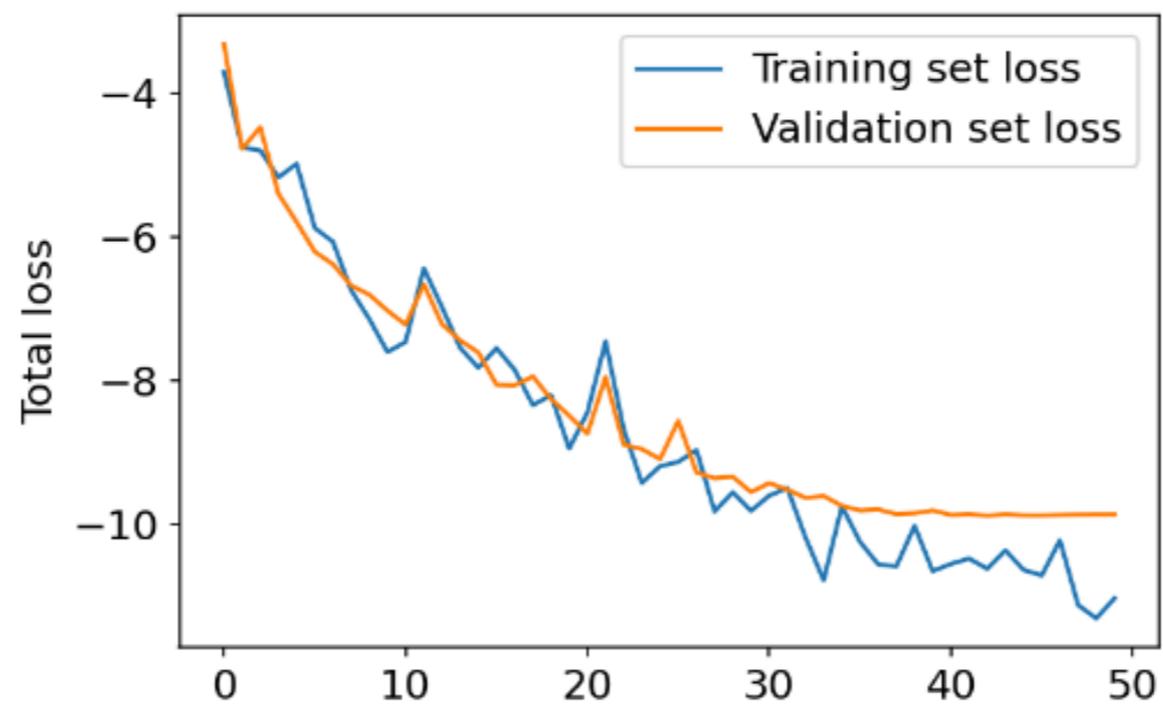
**Transferable kernel,**

$$p_{\theta, M}(\mathbf{x}) = \prod_{i=2}^N p_{\theta}(\mathbf{x}_i | \mathbf{C}_i)$$

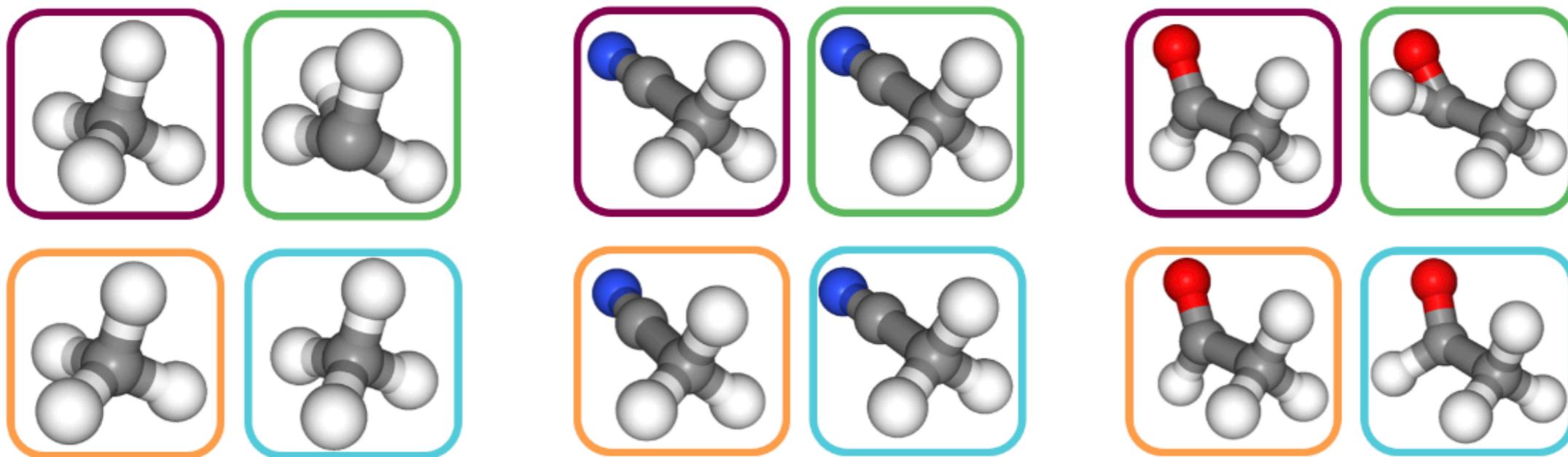
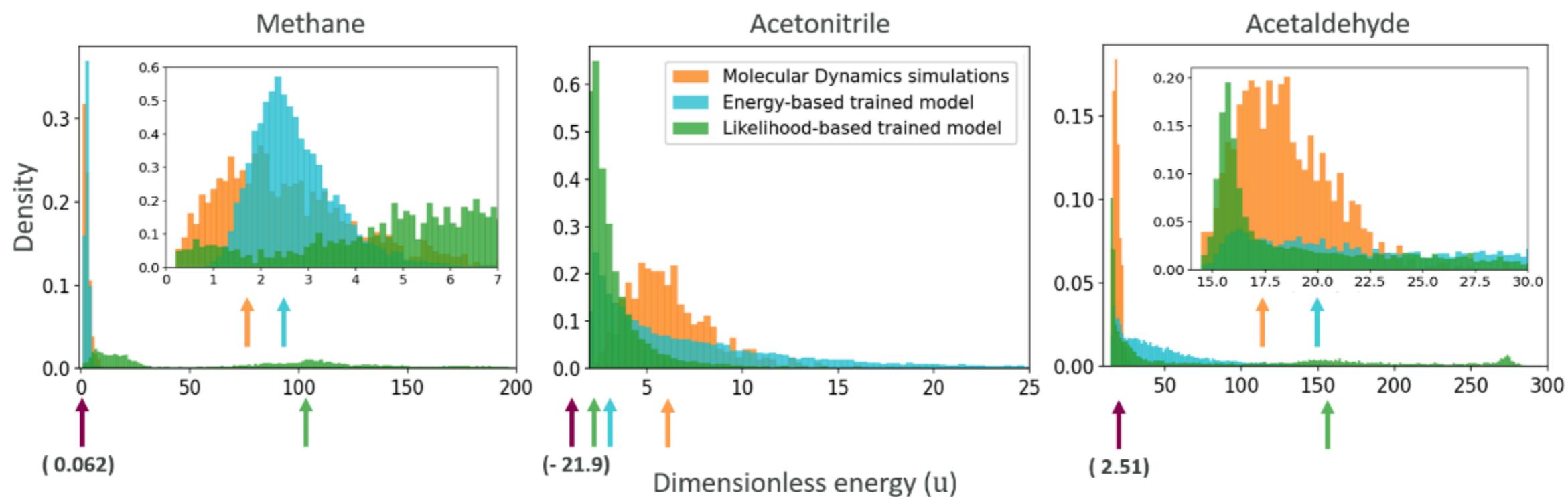
**With  $\mathbf{C}_i = (\mathbf{M}, \mathbf{A}_i, \mathbf{R}_{<i}, \mathbf{F}_i)$**



# Transferability



# Transferability



# Acknowledgements



Juan Viguera  
Diez



Tobias  
Karlsson



Christopher  
Kolloff



Vladimir  
Pastukhov

Azadeh Karimisefat & Dipti Aswal  
Enmin Su & Wenli Gao

